

# CSCI567 Machine Learning (Spring 2021)

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March 10, 2021

# Outline

- 1 Logistics
- 2 Review of last lecture
- 3 Boosting

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# Logistics

- Checkpoint 1 for project is due today. We will be tracking Kaggle submissions starting March 11, 2021.
- Quiz 1 has been graded. The mean, median, and standard deviation were 60.3, 62.3 and 17.4, respectively.
- March 12, 2021 is a **Wellness Day**, there will be no class.

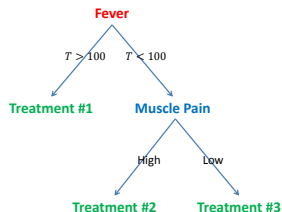
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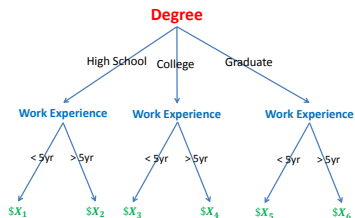
# Decision Trees

Many decisions are made based on some tree structure

## Medical treatment



## Salary in a company



# Learning Decision Trees

## DecisionTreeLearning(Examples, Features)

- if Examples have the same class, return a leaf with this class
- else if Features is empty, return a leaf with the majority class
- else if Examples is empty, return a leaf with majority class of parent
- else

find the best feature  $A$  to split (e.g. based on conditional entropy)

**Tree**  $\leftarrow$  a root with test on  $A$

For each value  $a$  of  $A$ :

**Child**  $\leftarrow$  DecisionTreeLearning(Examples with  $A = a$ , Features  $\setminus \{A\}$ )

add **Child** to **Tree** as a new branch

- return **Tree**

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  - Examples
  - AdaBoost
  - Derivation of AdaBoost



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We again focus on **binary classification**.

# A simple example

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- repeat ...
- final classifier is the **(weighted) majority vote** of all weak classifiers

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- many algorithms can deal with a **weighted training set** (e.g. for algorithm that minimizes some loss, we can simply **replace** “total loss” by “weighted total loss”)
- even if it's not obvious how to deal with weight directly, we can always **resample according to**  $D$  to create a new unweighted dataset

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**AdaBoost** is one of the most successful boosting algorithms.

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- update distributions

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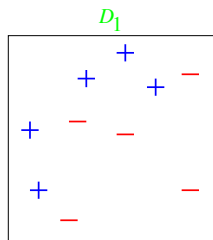
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Output the final classifier  $H(\mathbf{x}) = \text{sgn} \left( \sum_{t=1}^T \beta_t h_t(\mathbf{x}) \right)$

# Example

10 data points in  $\mathbb{R}^2$

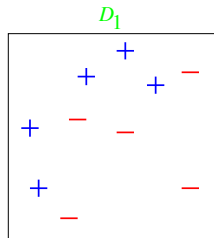
The size of  $+$  or  $-$  indicates the weight, which starts from uniform  $D_1$



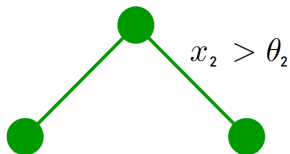
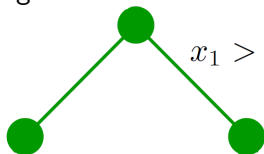
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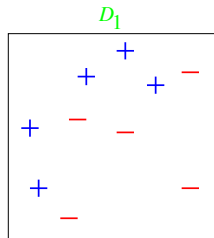
Base algorithm is decision stump:



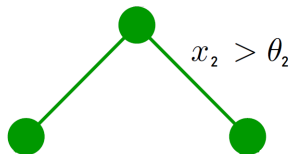
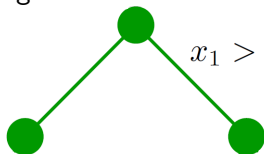
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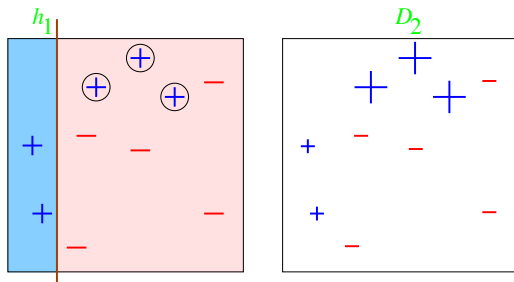
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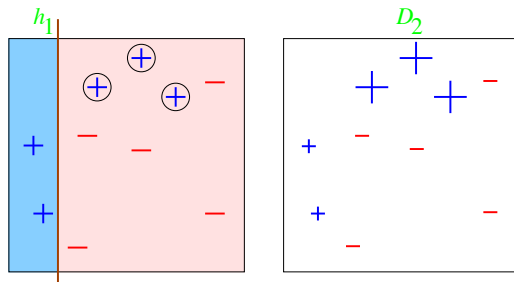
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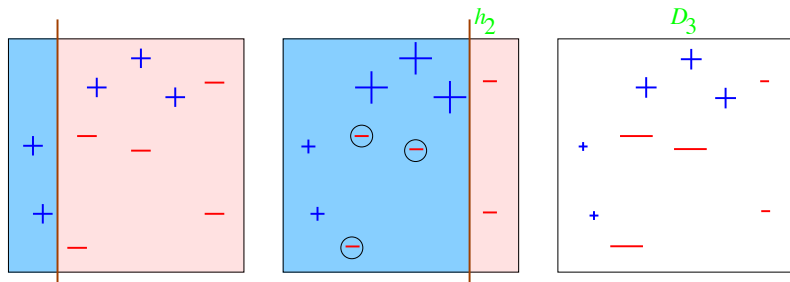
Observe that *no stump can predict very accurately for this dataset*

Round 1:  $t = 1$ 

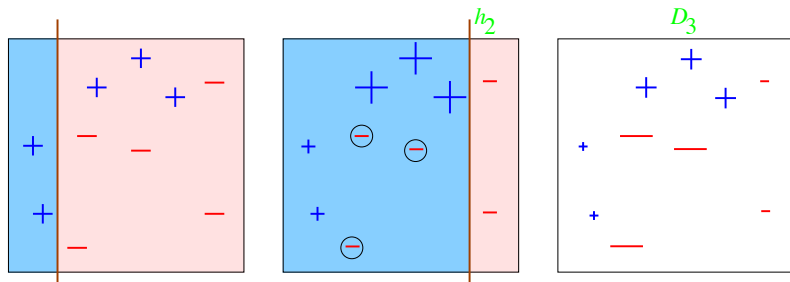
- 3 misclassified (circled):  $\epsilon_1 = 0.3 \rightarrow \beta_1 = \frac{1}{2} \ln \left( \frac{1-\epsilon_t}{\epsilon_t} \right) \approx 0.42$ .

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- $D_2$  puts more weights on those examples

Round 2:  $t = 2$ 

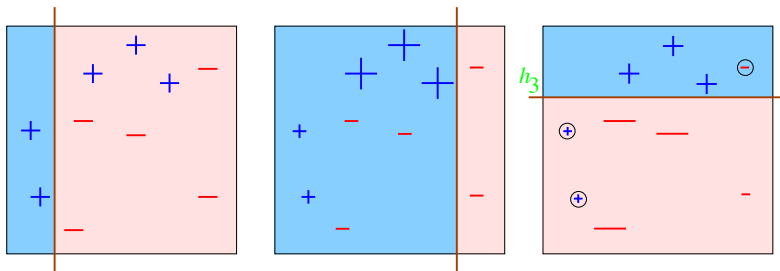
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- $D_3$  puts more weights on those examples

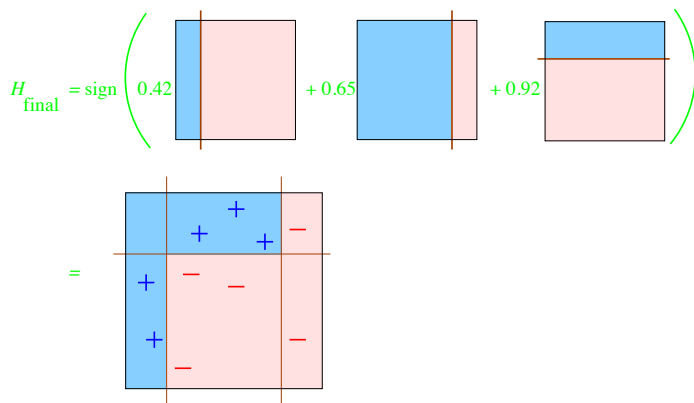


# Round 3: $t = 3$

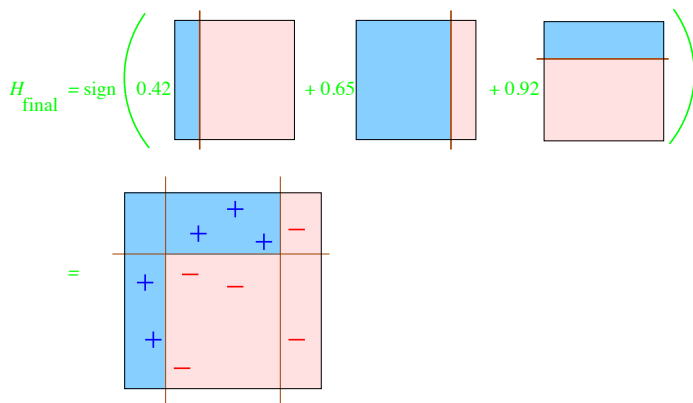


- again 3 misclassified (circled):  $\epsilon_3 = 0.14 \rightarrow \beta_3 = 0.92$ .

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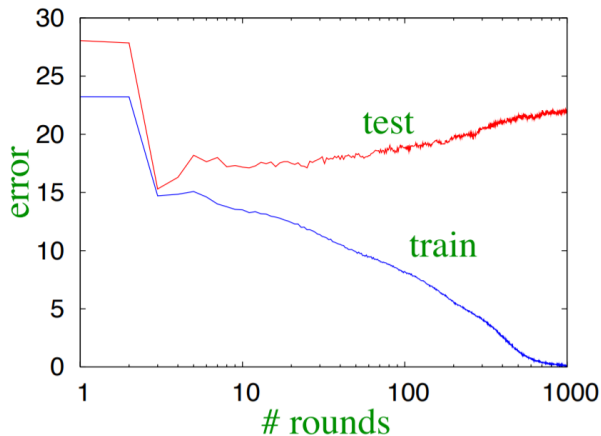
*All data points are now classified correctly*, even though each weak classifier makes 3 mistakes.

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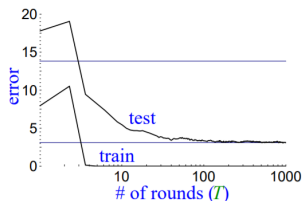
(boosting “stumps” on heart-disease dataset)

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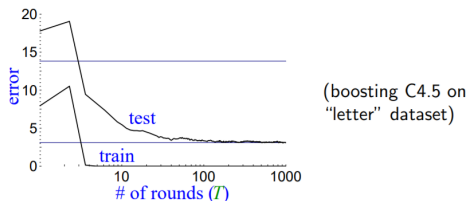
(boosting C4.5 on  
"letter" dataset)

- test error does **not** increase, even after 1000 rounds
  - (total size > 2,000,000 nodes)
- test error continues to drop even after training error is zero!

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Used to be a mystery, but by now rigorous theory has been developed to explain this phenomenon.



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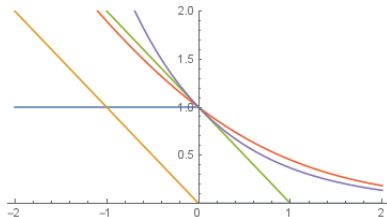
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Step 2: the loss that AdaBoost minimizes is the exponential loss

$$\sum_{n=1}^N \exp(-y_n f(\mathbf{x}_n))$$



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where the last step is by the definition of weights

$$D_t(n) \propto D_{t-1}(n) \exp(-y_n \beta_{t-1} h_{t-1}(\mathbf{x}_n)) \propto \dots \propto \exp(-y_n f_{t-1}(\mathbf{x}_n))$$

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So the goal becomes finding  $\beta_t, h_t \in \mathcal{H}$  that minimize

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This greedy step is abstracted out through a base algorithm.

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When  $h_t$  (and thus  $\epsilon_t$ ) is fixed, we then find  $\beta_t$  to minimize

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Keep doing this greedy minimization gives the AdaBoost algorithm.

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